

$$Ans1 = \begin{bmatrix} .1 = \left(\cos(15^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) & .2 = \left(\sin\left(\frac{7\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .3 = (\tan(75^\circ) = 2 + \sqrt{3}) & .4 = \left(\sin\left(\frac{23\pi}{12}\right) = \frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .5 = (\csc(-15^\circ) = -\sqrt{2}\sqrt{3} - \sqrt{2}) & .6 = (\tan(-195^\circ) = -2 + \sqrt{3}) \\ .7 = \left(\cot\left(-\frac{17\pi}{12}\right) = -2 + \sqrt{3} \right) & .8 = \left(\cos\left(-\frac{7\pi}{12}\right) = \frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) \end{bmatrix}$$

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$$Ans2 = \begin{bmatrix} .1 = \left(2 \sin(15^\circ) \cos(15^\circ) = \sin(30^\circ) = \frac{1}{2} \right) & .2 = \left(\cos(22.5^\circ)^2 - \sin(22.5^\circ)^2 = \cos(45^\circ) = \frac{\sqrt{2}}{2} \right) \\ .3 = \left(2 \cos\left(\frac{\pi}{12}\right) - 1 = \cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \right) & .4 = \left(\sin\left(\frac{\pi}{9}\right) \cos\left(\frac{5\pi}{36}\right) + \cos\left(\frac{\pi}{9}\right) \sin\left(\frac{5\pi}{36}\right) = \sin\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \\ .5 = \left(\frac{\tan(25^\circ) + \tan(5^\circ)}{1 - \tan(25^\circ) \tan(5^\circ)} = \tan(30^\circ) = \frac{\sqrt{3}}{3} \right) & .6 = \left(\frac{\tan\left(\frac{7\pi}{30}\right) - \tan\left(\frac{\pi}{15}\right)}{1 + \tan\left(\frac{7\pi}{30}\right) \tan\left(\frac{\pi}{15}\right)} = \tan\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{3} \right) \\ .7 = \left(\frac{2 \tan(22.5^\circ)}{1 - \tan(22.5^\circ)^2} = \tan(45^\circ) = 1 \right) & .8 = \left(\cos(70^\circ) \cos(10^\circ) + \sin(70^\circ) \sin(10^\circ) = \cos(60^\circ) = \frac{1}{2} \right) \\ .9 = (\cos(78^\circ) \cos(12^\circ) - \sin(78^\circ) \sin(12^\circ) = (\cos(90^\circ) = 0)) & .10 = \left(1 - 2 \sin\left(\frac{\pi}{8}\right)^2 = \cos\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \end{bmatrix}$$

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$$Ans3 = \begin{bmatrix} .1 = \left(\cos(\alpha) = \frac{\sqrt{39}}{8} \right) & .2 = \left(\sin(\beta) = -\frac{2\sqrt{2}}{3} \right) \\ .3 = \left(\tan(\alpha) = \frac{5\sqrt{39}}{39} \right) & .4 = \left(\sin(\beta - \alpha) = -\frac{\sqrt{39}\sqrt{2}}{12} + \frac{5}{24} \right) \\ .5 = \left(\cos(\alpha + \beta) = -\frac{\sqrt{39}}{24} + \frac{5\sqrt{2}}{12} \right) & .6 = \left(\tan(\alpha - \beta) = -\frac{45\sqrt{39}}{161} + \frac{128\sqrt{2}}{161} \right) \\ .7 = \left(\cos(2\beta) = \frac{-7}{9} \right) & .8 = \left(\tan(2\alpha) = \frac{5\sqrt{39}}{7} \right) \end{bmatrix}, Ans4 = \begin{bmatrix} .1 = \left(\cos(\alpha) = \frac{\sqrt{65}}{9} \right) & .2 = \left(\sin(\beta) = \frac{2\sqrt{10}}{7} \right) \\ .3 = \left(\tan(\beta) = -\frac{2\sqrt{10}}{3} \right) & .4 = \left(\sin(\alpha + \beta) = \frac{4}{21} + \frac{2\sqrt{65}\sqrt{10}}{63} \right) \\ .5 = \left(\cos(\beta - \alpha) = -\frac{\sqrt{65}}{21} - \frac{8\sqrt{10}}{63} \right) & .6 = \left(\tan(\alpha - \beta) = \frac{196\sqrt{5}\sqrt{13}}{55} - \frac{486\sqrt{5}\sqrt{2}}{55} \right) \\ .7 = \left(\sin(2\alpha) = -\frac{8\sqrt{65}}{81} \right) & .8 = \left(\tan(2\beta) = \frac{12\sqrt{10}}{31} \right) \end{bmatrix}$$

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$$Ans5 = (\sin(17^\circ) = (\text{sqrt}(0.0855) = 0.292)), \begin{bmatrix} M \\ U \\ T \end{bmatrix}$$

$$Ans6 = (\cos(39^\circ) = (\text{sqrt}(0.6040) = 0.777)), \begin{bmatrix} M \\ U \\ T \end{bmatrix}$$

$$Ans1 = \begin{bmatrix} .1 = \left(\cos\left(\frac{\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) & .2 = \left(\sin(105^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .3 = \left(\tan\left(\frac{5\pi}{12}\right) = 2 + \sqrt{3} \right) & .4 = \left(\sin\left(-\frac{19\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .5 = \left(\cos((-75)^\circ) = \frac{\sqrt{2}\sqrt{3}}{4} - \frac{\sqrt{2}}{4} \right) & .6 = \left(\cot\left(\frac{23\pi}{12}\right) = -2 - \sqrt{3} \right) \\ .7 = (\sec(-195)^\circ) = -\sqrt{2}\sqrt{3} + \sqrt{2} & .8 = \left(\csc\left(\frac{11\pi}{12}\right) = \sqrt{2}\sqrt{3} + \sqrt{2} \right) \end{bmatrix}$$

$$Ans2 = \begin{bmatrix} .1 = \left(\frac{2 \tan(22.5^\circ)}{1 - \tan(22.5^\circ)^2} = (\tan(45^\circ) = 1) \right) & .2 = \left(\frac{\tan(70^\circ) - \tan(10^\circ)}{1 + \tan(70^\circ) \tan(10^\circ)} = (\tan(60^\circ) = \sqrt{3}) \right) \\ .3 = \left(1 - 2 \sin\left(\frac{\pi}{8}\right) = \left(\cos\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \right) & .4 = \left(2 \cos(15^\circ)^2 - 1 = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) \\ .5 = \left(2 \sin\left(\frac{\pi}{12}\right) \cos\left(\frac{\pi}{12}\right) = \left(\sin\left(\frac{\pi}{6}\right) = \frac{1}{2} \right) \right) & .6 = \left(\sin(30^\circ) \cos(15^\circ) + \cos(30^\circ) \sin(15^\circ) = \left(\sin(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \\ .7 = \left(\frac{\tan\left(\frac{5\pi}{36}\right) + \tan\left(\frac{\pi}{36}\right)}{1 - \tan\left(\frac{5\pi}{36}\right) \tan\left(\frac{\pi}{36}\right)} = \left(\tan\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{3} \right) \right) & .8 = \left(\cos(22.5^\circ)^2 - \sin(22.5^\circ)^2 = \left(\cos(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \\ .9 = \left(\cos\left(\frac{2\pi}{9}\right) \cos\left(\frac{\pi}{18}\right) + \sin\left(\frac{2\pi}{9}\right) \sin\left(\frac{\pi}{18}\right) = \left(\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \right) \right) & .10 = \left(\cos\left(\frac{2\pi}{9}\right) \cos\left(\frac{\pi}{9}\right) - \sin\left(\frac{2\pi}{9}\right) \sin\left(\frac{\pi}{9}\right) = \left(\cos\left(\frac{\pi}{3}\right) = \frac{1}{2} \right) \right) \end{bmatrix}$$

$$Ans3 = \begin{bmatrix} .1 = \left(\cos(\alpha) = \frac{\sqrt{7}}{4} \right) & .2 = \left(\sin(\beta) = \frac{2\sqrt{10}}{7} \right) \\ .3 = \left(\tan(\alpha) = \frac{3\sqrt{7}}{7} \right) & .4 = \left(\sin(\alpha + \beta) = -\frac{9}{28} + \frac{\sqrt{7}\sqrt{10}}{14} \right) \\ .5 = \left(\cos(\beta - \alpha) = -\frac{3\sqrt{7}}{28} + \frac{3\sqrt{10}}{14} \right) & .6 = \left(\tan(\alpha - \beta) = -\frac{49\sqrt{7}}{99} - \frac{32\sqrt{10}}{99} \right) \\ .7 = \left(\sin(2\alpha) = \frac{3\sqrt{7}}{8} \right) & .8 = \left(\tan(2\beta) = \frac{12\sqrt{10}}{31} \right) \end{bmatrix}, Ans4 = \begin{bmatrix} .1 = \left(\cos(\alpha) = \frac{\sqrt{15}}{4} \right) & .2 = \left(\sin(\beta) = \frac{-4}{5} \right) \\ .3 = \left(\tan(\alpha) = -\frac{\sqrt{15}}{15} \right) & .4 = \left(\sin(\alpha + \beta) = \frac{3}{20} - \frac{\sqrt{15}}{5} \right) \\ .5 = \left(\cos(\alpha - \beta) = -\frac{3\sqrt{15}}{20} + \frac{1}{5} \right) & .6 = \left(\tan(\beta - \alpha) = \frac{192}{119} + \frac{25\sqrt{15}}{119} \right) \\ .7 = \left(\cos(2\beta) = \frac{-7}{25} \right) & .8 = \left(\tan(2\alpha) = -\frac{\sqrt{15}}{7} \right) \end{bmatrix}$$

Ans5 = (Cos(4°) = (Sqrt(0.9950) = 0.998)),
 Ans6 = (Sin(41°) = (Sqrt(0.4305) = 0.656)),

$$Ans1 = \left[\begin{array}{ll} .1 = \left(\sin\left(\frac{5\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) & .2 = \left(\cos(15^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .3 = \left(\tan(105^\circ) = -2 - \sqrt{3} \right) & .4 = \left(\sin((-255)^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .5 = \left(\sec\left(-\frac{19\pi}{12}\right) = \sqrt{2}\sqrt{3} + \sqrt{2} \right) & .6 = \left(\tan((-345)^\circ) = 2 - \sqrt{3} \right) \\ .7 = \left(\cot\left(-\frac{13\pi}{12}\right) = -2 - \sqrt{3} \right) & .8 = \left(\csc(255^\circ) = -\sqrt{2}\sqrt{3} + \sqrt{2} \right) \end{array} \right], \begin{array}{l} \frac{:] \\ :(\ \\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \frac{:] \\ :(\ \end{array}$$

$$Ans2 = \left[\begin{array}{ll} .1 = \left(\frac{\tan(55^\circ) - \tan(10^\circ)}{1 + \tan(55^\circ)\tan(10^\circ)} = \left(\tan(45^\circ) = 1 \right) \right) & .2 = \left(\cos\left(\frac{11\pi}{18}\right)\cos\left(\frac{\pi}{9}\right) + \sin\left(\frac{11\pi}{18}\right)\sin\left(\frac{\pi}{9}\right) = \left(\cos\left(\frac{\pi}{2}\right) = 0 \right) \right) \\ .3 = \left(\sin(72^\circ)\cos(12^\circ) - \cos(72^\circ)\sin(12^\circ) = \left(\sin(60^\circ) = \frac{\sqrt{3}}{2} \right) \right) & .4 = \left(2\cos\left(\frac{\pi}{12}\right)^2 - 1 = \left(\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \right) \right) \\ .5 = \left(2\sin(22.5^\circ)\cos(22.5^\circ) = \left(\sin(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) & .6 = \left(\frac{2\tan(22.5^\circ)}{1 - \tan(22.5^\circ)^2} = \left(\tan(45^\circ) = 1 \right) \right) \\ .7 = \left(\frac{\tan\left(\frac{\pi}{9}\right) + \tan\left(\frac{\pi}{18}\right)}{1 - \tan\left(\frac{\pi}{9}\right)\tan\left(\frac{\pi}{18}\right)} = \left(\tan\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{3} \right) \right) & .8 = \left(\cos\left(\frac{\pi}{8}\right)^2 - \sin\left(\frac{\pi}{8}\right)^2 = \left(\cos\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \right) \\ .9 = \left(1 - 2\sin(15^\circ)^2 = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) & .10 = \left(\sin(12^\circ)\cos(33^\circ) + \cos(12^\circ)\sin(33^\circ) = \left(\sin(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \end{array} \right], \begin{array}{l} \frac{:] \\ :(\ \\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \frac{:] \\ :(\ \\ \frac{:] \\ :(\ \\ \frac{:] \\ :(\ \end{array}$$

$$Ans3 = \left[\begin{array}{ll} .1 = \left(\sin(\alpha) = \frac{3\sqrt{5}}{7} \right) & .2 = \left(\cos(\beta) = \frac{\sqrt{65}}{9} \right) \\ .3 = \left(\tan(\beta) = -\frac{4\sqrt{65}}{65} \right) & .4 = \left(\sin(\beta - \alpha) = -\frac{8}{63} - \frac{\sqrt{5}\sqrt{65}}{21} \right) \\ .5 = \left(\cos(\alpha - \beta) = \frac{2\sqrt{65}}{63} - \frac{4\sqrt{5}}{21} \right) & .6 = \left(\tan(\alpha + \beta) = -\frac{243\sqrt{5}}{230} + \frac{49\sqrt{5}\sqrt{13}}{115} \right) \\ .7 = \left(\sin(2\beta) = -\frac{8\sqrt{65}}{81} \right) & .8 = \left(\tan(2\alpha) = -\frac{12\sqrt{5}}{41} \right) \end{array} \right], \quad Ans4 = \left[\begin{array}{ll} .1 = \left(\sin(\alpha) = \frac{2\sqrt{14}}{9} \right) & .2 = \left(\cos(\beta) = -\frac{2\sqrt{6}}{5} \right) \\ .3 = \left(\tan(\beta) = \frac{\sqrt{6}}{12} \right) & .4 = \left(\sin(\alpha + \beta) = -\frac{4\sqrt{14}\sqrt{6}}{45} + \frac{1}{9} \right) \\ .5 = \left(\cos(\alpha - \beta) = \frac{2\sqrt{6}}{9} - \frac{2\sqrt{14}}{45} \right) & .6 = \left(\tan(\beta - \alpha) = \frac{81\sqrt{2}\sqrt{3}}{272} + \frac{125\sqrt{2}\sqrt{7}}{272} \right) \\ .7 = \left(\cos(2\alpha) = \frac{-31}{81} \right) & .8 = \left(\tan(2\beta) = \frac{4\sqrt{6}}{23} \right) \end{array} \right], \begin{array}{l} \frac{:] \\ :(\ \\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \frac{:] \\ :(\ \end{array}$$

$$Ans5 = (\sin(18^\circ) = (\text{Sqrt}(0.0955) = 0.309)), \begin{array}{l} M \\ U \\ T \end{array}$$

$$Ans6 = (\cos(31^\circ) = (\text{Sqrt}(0.7345) = 0.857)), \begin{array}{l} M \\ U \\ T \end{array}$$

$$\text{Ans1} = \begin{matrix} .1 = \left(\sin\left(\frac{7\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) & .2 = \left(\cos(75^\circ) = \frac{\sqrt{2}\sqrt{3}}{4} - \frac{\sqrt{2}}{4} \right) \\ .3 = \left(\tan\left(\frac{\pi}{12}\right) = 2 - \sqrt{3} \right) & .4 = \left(\cos(-255^\circ) = \frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .5 = \left(\sin\left(-\frac{5\pi}{12}\right) = -\frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) & .6 = \left(\cot\left(\frac{17\pi}{12}\right) = 2 - \sqrt{3} \right) \\ .7 = \left(\tan(-195^\circ) = -2 + \sqrt{3} \right) & .8 = \left(\csc(-345^\circ) = \sqrt{2}\sqrt{3} + \sqrt{2} \right) \end{matrix} \cdot \left[\begin{matrix} \div \\ \cdot \\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \div \\ \cdot \end{matrix} \right]$$

$$\text{Ans2} = \begin{matrix} .1 = \left(\sin(48^\circ)\cos(12^\circ) + \cos(48^\circ)\sin(12^\circ) = \left(\sin(60^\circ) = \frac{\sqrt{3}}{2}\right) \right) & .2 = \left(\cos\left(\frac{\pi}{8}\right)^2 - \sin\left(\frac{\pi}{8}\right)^2 = \left(\cos\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2}\right) \right) \\ .3 = \left(\frac{2\tan\left(\frac{\pi}{8}\right)}{1 - \tan\left(\frac{\pi}{8}\right)^2} = \left(\tan\left(\frac{\pi}{4}\right) = \tan\left(\frac{\pi}{4}\right)\right) \right) & .4 = \left(\cos\left(\frac{17\pi}{36}\right)\cos\left(\frac{5\pi}{36}\right) + \sin\left(\frac{17\pi}{36}\right)\sin\left(\frac{5\pi}{36}\right) = \left(\cos\left(\frac{\pi}{3}\right) = \frac{1}{2}\right) \right) \\ .5 = \left(1 - 2\sin(15^\circ)^2 = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2}\right) \right) & .6 = \left(2\sin\left(\frac{\pi}{12}\right)\cos\left(\frac{\pi}{12}\right) = \left(\sin\left(\frac{\pi}{6}\right) = \frac{1}{2}\right) \right) \\ .7 = \left(2\cos(22.5^\circ)^2 - 1 = \left(\cos(45^\circ) = \frac{\sqrt{2}}{2}\right) \right) & .8 = \left(\cos\left(\frac{\pi}{9}\right)\cos\left(\frac{\pi}{18}\right) - \sin\left(\frac{\pi}{9}\right)\sin\left(\frac{\pi}{18}\right) = \left(\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}\right) \right) \\ .9 = \left(\sin(42^\circ)\cos(12^\circ) - \cos(42^\circ)\sin(12^\circ) = \left(\sin(30^\circ) = \frac{1}{2}\right) \right) & .10 = \left(\frac{\tan\left(\frac{5\pi}{36}\right) + \tan\left(\frac{\pi}{9}\right)}{1 - \tan\left(\frac{5\pi}{36}\right)\tan\left(\frac{\pi}{9}\right)} = \left(\tan\left(\frac{\pi}{4}\right) = 1\right) \right) \end{matrix} \cdot \left[\begin{matrix} \div \\ \cdot \\ \div \\ \cdot \\ \left[\begin{matrix} M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \end{matrix} \right] \\ \div \\ \cdot \\ \div \\ \cdot \end{matrix} \right]$$

$$\text{Ans3} = \begin{matrix} .1 = \left(\cos(\alpha) = \frac{\sqrt{35}}{6} \right) & .2 = \left(\sin(\beta) = \frac{2\sqrt{10}}{7} \right) \\ .3 = \left(\tan(\alpha) = \frac{\sqrt{35}}{35} \right) & .4 = \left(\sin(\beta - \alpha) = \frac{\sqrt{35}\sqrt{10}}{21} + \frac{1}{14} \right) \\ .5 = \left(\cos(\alpha + \beta) = -\frac{\sqrt{35}}{14} - \frac{\sqrt{10}}{21} \right) & .6 = \left(\tan(\alpha - \beta) = \frac{49\sqrt{5}\sqrt{7}}{275} + \frac{216\sqrt{5}\sqrt{2}}{275} \right) \\ .7 = \left(\sin(2\alpha) = \frac{\sqrt{35}}{18} \right) & .8 = \left(\tan(2\beta) = \frac{12\sqrt{10}}{31} \right) \end{matrix} \cdot \text{Ans4} = \begin{matrix} .1 = \left(\sin(\alpha) = -\frac{\sqrt{21}}{5} \right) & .2 = \left(\cos(\beta) = \frac{\sqrt{3}}{2} \right) \\ .3 = \left(\tan(\beta) = -\frac{\sqrt{3}}{3} \right) & .4 = \left(\sin(\beta - \alpha) = \frac{1}{5} + \frac{\sqrt{21}\sqrt{3}}{10} \right) \\ .5 = \left(\cos(\alpha - \beta) = -\frac{\sqrt{3}}{5} + \frac{\sqrt{21}}{10} \right) & .6 = \left(\tan(\alpha + \beta) = -\frac{8\sqrt{7}\sqrt{3}}{9} + \frac{25\sqrt{3}}{9} \right) \\ .7 = \left(\cos(2\alpha) = \frac{-17}{25} \right) & .8 = \left(\tan(2\beta) = -\sqrt{3} \right) \end{matrix} \cdot \left[\begin{matrix} \div \\ \cdot \\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \div \\ \cdot \end{matrix} \right]$$

$$\text{Ans5} = (\cos(37^\circ) = (\text{sqrt}(0.6380) = 0.799)), \cdot \left[\begin{matrix} M \\ U \\ T \end{matrix} \right]$$

$$\text{Ans6} = (\sin(6^\circ) = (\text{sqrt}(0.0110) = 0.105)), \cdot \left[\begin{matrix} M \\ U \\ T \end{matrix} \right]$$

$$Ans1 = \left[\begin{array}{l} .1 = \left(\sin(105^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .2 = \left(\cos\left(\frac{\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .3 = \left(\tan(75^\circ) = 2 + \sqrt{3} \right) \\ .4 = \left(\csc((-15)^\circ) = -\sqrt{2}\sqrt{3} - \sqrt{2} \right) \\ .5 = \left(\sec\left(\frac{13\pi}{12}\right) = -\sqrt{2}\sqrt{3} + \sqrt{2} \right) \\ .6 = \left(\cot\left(-\frac{7\pi}{12}\right) = 2 - \sqrt{3} \right) \\ .7 = \left(\tan((-195)^\circ) = -2 + \sqrt{3} \right) \\ .8 = \left(\cos((-165)^\circ) = -\frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) \end{array} \right], \begin{array}{l} \div \\ : \\ (\\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \div \\ : \\ (\end{array}$$

$$Ans2 = \left[\begin{array}{l} .1 = \left(\cos(15^\circ)^2 - \sin(15^\circ)^2 = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) \\ .2 = \left(\sin\left(\frac{7\pi}{18}\right) \cos\left(\frac{\pi}{9}\right) + \cos\left(\frac{7\pi}{18}\right) \sin\left(\frac{\pi}{9}\right) = \left(\sin\left(\frac{\pi}{2}\right) = 1 \right) \right) \\ .3 = \left(\frac{\tan\left(\frac{5\pi}{18}\right) - \tan\left(\frac{\pi}{9}\right)}{1 + \tan\left(\frac{5\pi}{18}\right) \tan\left(\frac{\pi}{9}\right)} = \left(\tan\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{3} \right) \right) \\ .4 = \left(\cos(20^\circ) \cos(10^\circ) - \sin(20^\circ) \sin(10^\circ) = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) \\ .5 = \left(2 \sin\left(\frac{\pi}{12}\right) \cos\left(\frac{\pi}{12}\right) = \left(\sin\left(\frac{\pi}{6}\right) = \frac{1}{2} \right) \right) \\ .6 = \left(\frac{2 \tan(22.5^\circ)}{1 - \tan(22.5^\circ)^2} = \left(\tan(45^\circ) = 1 \right) \right) \\ .7 = \left(\frac{\tan(12^\circ) + \tan(33^\circ)}{1 - \tan(12^\circ) \tan(33^\circ)} = \left(\tan(45^\circ) = 1 \right) \right) \\ .8 = \left(\cos(70^\circ) \cos(10^\circ) + \sin(70^\circ) \sin(10^\circ) = \left(\cos(60^\circ) = \frac{1}{2} \right) \right) \\ .9 = \left(1 - 2 \sin\left(\frac{\pi}{8}\right)^2 = \left(\cos\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \right) \\ .10 = \left(2 \cos(22.5^\circ)^2 - 1 = \left(\cos(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \end{array} \right], \begin{array}{l} \div \\ : \\ (\\ \div \\ : \\ (\\ \left[\begin{array}{l} M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \end{array} \right] \\ \div \\ : \\ (\\ \div \\ : \\ (\\ \div \\ : \\ (\end{array}$$

$$Ans3 = \left[\begin{array}{l} .1 = \left(\sin(\alpha) = \frac{\sqrt{21}}{5} \right) \\ .2 = \left(\cos(\beta) = \frac{-3}{5} \right) \\ .3 = \left(\tan(\alpha) = \frac{\sqrt{21}}{2} \right) \\ .4 = \left(\sin(\alpha + \beta) = -\frac{3\sqrt{21}}{25} + \frac{8}{25} \right) \\ .5 = \left(\cos(\alpha - \beta) = -\frac{6}{25} + \frac{4\sqrt{21}}{25} \right) \\ .6 = \left(\tan(\beta - \alpha) = 1 + \frac{\sqrt{21}}{6} \right) \\ .7 = \left(\sin(2\beta) = \frac{-24}{25} \right) \\ .8 = \left(\tan(2\alpha) = -\frac{4\sqrt{21}}{17} \right) \end{array} \right], Ans4 = \left[\begin{array}{l} .1 = \left(\sin(\alpha) = -\frac{2\sqrt{6}}{7} \right) \\ .2 = \left(\cos(\beta) = -\frac{2\sqrt{2}}{3} \right) \\ .3 = \left(\tan(\alpha) = -\frac{2\sqrt{6}}{5} \right) \\ .4 = \left(\sin(\beta - \alpha) = -\frac{5}{21} - \frac{4\sqrt{6}\sqrt{2}}{21} \right) \\ .5 = \left(\cos(\alpha - \beta) = -\frac{10\sqrt{2}}{21} + \frac{2\sqrt{6}}{21} \right) \\ .6 = \left(\tan(\alpha + \beta) = -\frac{45\sqrt{2}\sqrt{3}}{88} + \frac{49\sqrt{2}}{88} \right) \\ .7 = \left(\cos(2\beta) = \frac{7}{9} \right) \\ .8 = \left(\tan(2\alpha) = -20\sqrt{6} \right) \end{array} \right], \begin{array}{l} \div \\ : \\ (\\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \div \\ : \\ (\end{array}$$

$$Ans5 = (\sin(19^\circ) = (\text{Sqrt}(0.1060) = 0.326)), \begin{array}{l} M \\ U \\ T \end{array}$$

$$Ans6 = (\cos(8^\circ) = (\text{Sqrt}(0.9805) = 0.990)), \begin{array}{l} M \\ U \\ T \end{array}$$

$$\text{Ans1} = \left[\begin{array}{l} .1 = \left(\sin(105^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \quad .2 = \left(\cos\left(\frac{\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .3 = (\tan(75^\circ) = 2 + \sqrt{3}) \quad .4 = \left(\cot\left(-\frac{7\pi}{12}\right) = 2 - \sqrt{3} \right) \\ .5 = (\csc(-165^\circ) = -\sqrt{2}\sqrt{3} - \sqrt{2}) \quad .6 = \left(\cos\left(\frac{13\pi}{12}\right) = -\frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .7 = (\tan(-255^\circ) = -2 - \sqrt{3}) \quad .8 = \left(\sin(-285^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \end{array} \right], \left[\begin{array}{c} \div \\ : \\ (\\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \div \\ : \\ (\end{array} \right]$$

$$\text{Ans2} = \left[\begin{array}{l} .1 = \left(\sin\left(\frac{\pi}{36}\right)\cos\left(\frac{5\pi}{36}\right) + \cos\left(\frac{\pi}{36}\right)\sin\left(\frac{5\pi}{36}\right) = \left(\sin\left(\frac{\pi}{6}\right) = \frac{1}{2} \right) \right) \quad .2 = \left(\sin(65^\circ)\cos(20^\circ) - \cos(65^\circ)\sin(20^\circ) = \left(\sin(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \\ .3 = \left(\cos(22.5^\circ)^2 - \sin(22.5^\circ)^2 = \left(\cos(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \quad .4 = \left(1 - 2\sin\left(\frac{\pi}{8}\right)^2 = \left(\cos\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \right) \\ .5 = \left(\frac{2 \tan\left(\frac{\pi}{8}\right)}{1 - \tan\left(\frac{\pi}{8}\right)^2} = \left(\tan\left(\frac{\pi}{4}\right) = \tan\left(\frac{\pi}{4}\right) \right) \right) \quad .6 = \left(2 \sin(15^\circ)\cos(15^\circ) = \left(\sin(30^\circ) = \frac{1}{2} \right) \right) \\ .7 = \left(2 \cos\left(\frac{\pi}{12}\right)^2 - 1 = \left(\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \right) \right) \quad .8 = \left(\frac{\tan(80^\circ) - \tan(20^\circ)}{1 + \tan(80^\circ)\tan(20^\circ)} = \left(\tan(60^\circ) = \sqrt{3} \right) \right) \\ .9 = \left(\frac{\tan\left(\frac{4\pi}{15}\right) + \tan\left(\frac{\pi}{15}\right)}{1 - \tan\left(\frac{4\pi}{15}\right)\tan\left(\frac{\pi}{15}\right)} = \left(\tan\left(\frac{\pi}{3}\right) = \sqrt{3} \right) \right) \quad .10 = \left(\cos\left(\frac{7\pi}{36}\right)\cos\left(\frac{\pi}{36}\right) + \sin\left(\frac{7\pi}{36}\right)\sin\left(\frac{\pi}{36}\right) = \left(\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \right) \right) \end{array} \right], \left[\begin{array}{c} \div \\ : \\ (\\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \div \\ : \\ (\end{array} \right]$$

$$\text{Ans3} = \left[\begin{array}{l} .1 = \left(\sin(\alpha) = \frac{2\sqrt{2}}{3} \right) \quad .2 = \left(\cos(\beta) = \frac{2\sqrt{14}}{9} \right) \\ .3 = (\tan(\alpha) = 2\sqrt{2}) \quad .4 = \left(\sin(\alpha - \beta) = \frac{4\sqrt{2}\sqrt{14} + 5}{27} \right) \\ .5 = \left(\cos(\beta - \alpha) = -\frac{10\sqrt{2}}{27} + \frac{2\sqrt{14}}{27} \right) \quad .6 = \left(\tan(\alpha + \beta) = -\frac{9\sqrt{2}}{8} + \frac{5\sqrt{2}\sqrt{7}}{8} \right) \\ .7 = \left(\cos(2\beta) = \frac{31}{81} \right) \quad .8 = \left(\tan(2\alpha) = -\frac{4\sqrt{2}}{7} \right) \end{array} \right], \text{Ans4} = \left[\begin{array}{l} .1 = \left(\sin(\alpha) = -\frac{\sqrt{21}}{5} \right) \quad .2 = \left(\cos(\beta) = -\frac{\sqrt{7}}{4} \right) \\ .3 = \left(\tan(\beta) = -\frac{3\sqrt{7}}{7} \right) \quad .4 = \left(\sin(\alpha - \beta) = \frac{\sqrt{21}\sqrt{7} + 3}{20} \right) \\ .5 = \left(\cos(\alpha + \beta) = \frac{\sqrt{7}}{10} + \frac{3\sqrt{21}}{20} \right) \quad .6 = \left(\tan(\beta - \alpha) = \frac{75\sqrt{7}}{161} + \frac{32\sqrt{7}\sqrt{3}}{161} \right) \\ .7 = \left(\cos(2\beta) = \frac{-1}{8} \right) \quad .8 = \left(\tan(2\alpha) = -\frac{4\sqrt{21}}{17} \right) \end{array} \right], \left[\begin{array}{c} \div \\ : \\ (\\ M \\ a \\ t \\ h \\ @ \\ M \\ U \\ T \\ \div \\ : \\ (\end{array} \right]$$

$$\text{Ans5} = (\cos(21^\circ) = (\text{Sqrt}(0.8715) = 0.934)), \left[\begin{array}{c} M \\ U \\ T \end{array} \right]$$

$$\text{Ans6} = (\sin(5^\circ) = (\text{Sqrt}(0.0075) = 0.087)), \left[\begin{array}{c} M \\ U \\ T \end{array} \right]$$

Ans1 = [.1 = Cos(7pi/12) = sqrt(2)/4 - sqrt(2)*sqrt(3)/4, .2 = Sin(75 degrees) = sqrt(2)/4 + sqrt(2)*sqrt(3)/4, .3 = Tan(pi/12) = 2 - sqrt(3), .4 = Cos(-5pi/12) = sqrt(2)*sqrt(3)/4 - sqrt(2)/4, .5 = Sec((-345 degrees)) = sqrt(2)*sqrt(3) - sqrt(2), .6 = Cot(-11pi/12) = 2 + sqrt(3), .7 = Tan((-285 degrees)) = 2 + sqrt(3), .8 = Csc(255 degrees) = -sqrt(2)*sqrt(3) + sqrt(2)]

Ans2 = [.1 = Sin(100 degrees) Cos(10 degrees) - Cos(100 degrees) Sin(10 degrees) = Sin(90 degrees) = 1, .2 = 2 Sin(22.5 degrees) Cos(22.5 degrees) = Sin(45 degrees) = sqrt(2)/2, .3 = Cos(15 degrees)^2 - Sin(15 degrees)^2 = Cos(30 degrees) = sqrt(3)/2, .4 = 2 Cos(pi/8)^2 - 1 = Cos(pi/4) = sqrt(2)/2, .5 = (Tan(5pi/18) - Tan(pi/9)) / (1 + Tan(5pi/18)Tan(pi/9)) = Tan(pi/6) = sqrt(3)/3, .6 = (Tan(pi/15) + Tan(pi/10)) / (1 - Tan(pi/15)Tan(pi/10)) = Tan(pi/6) = sqrt(3)/3, .7 = (2 Tan(22.5 degrees)^2) / (1 - Tan(22.5 degrees)^2) = Tan(45 degrees) = 1, .8 = Sin(35 degrees) Cos(25 degrees) + Cos(35 degrees) Sin(25 degrees) = Sin(60 degrees) = sqrt(3)/2, .9 = Cos(pi/12) Cos(pi/6) - Sin(pi/12) Sin(pi/6) = Cos(pi/4) = sqrt(2)/2, .10 = (1 - 2 Sin(pi/12)^2) = Cos(pi/6) = sqrt(3)/2]

Ans3 = [.1 = Sin(alpha) = sqrt(5)/3, .2 = Cos(beta) = -sqrt(3)/2, .3 = Tan(alpha) = sqrt(5)/2, .4 = Sin(alpha - beta) = (-sqrt(3)*sqrt(5)/6 + 1/3), .5 = Cos(alpha + beta) = (-sqrt(3)/3 + sqrt(5)/6), .6 = Tan(beta - alpha) = (9*sqrt(3)/7 - 8*sqrt(5)/7), .7 = Cos(2 beta) = 1/2, .8 = Tan(2 alpha) = -4*sqrt(5)]

Ans4 = [.1 = Sin(alpha) = sqrt(7)/4, .2 = Cos(beta) = sqrt(65)/9, .3 = Tan(beta) = -4*sqrt(65)/65, .4 = Sin(beta - alpha) = (1/3 - sqrt(7)*sqrt(65)/36), .5 = Cos(alpha - beta) = (-sqrt(65)/12 - sqrt(7)/9), .6 = Tan(alpha + beta) = (-243*sqrt(7)/473 - 64*sqrt(65)/473), .7 = Cos(2 beta) = 49/81, .8 = Tan(2 alpha) = -3*sqrt(7)]

Ans5 = (Sin(23 degrees) = Sqrt(0.1525) = 0.391),

Ans6 = (Cos(5 degrees) = Sqrt(0.9925) = 0.996),

$$Ans1 = \begin{bmatrix} .1 = \left(\cos(15^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) & .2 = \left(\sin\left(\frac{5\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .3 = (\tan(105^\circ) = -2 - \sqrt{3}) & .4 = \left(\sin(-285^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .5 = \left(\sec\left(-\frac{7\pi}{12}\right) = -\sqrt{2}\sqrt{3} - \sqrt{2} \right) & .6 = (\csc(-75^\circ) = -\sqrt{2}\sqrt{3} + \sqrt{2}) \\ .7 = \left(\tan\left(-\frac{\pi}{12}\right) = -2 + \sqrt{3} \right) & .8 = \left(\cos\left(\frac{23\pi}{12}\right) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \end{bmatrix}, \begin{bmatrix} \text{.} \\ \text{:} \\ \text{M} \\ \text{a} \\ \text{t} \\ \text{h} \\ \text{.} \\ \text{@} \\ \text{M} \\ \text{U} \\ \text{T} \\ \text{.} \\ \text{:} \end{bmatrix}$$

$$Ans2 = \begin{bmatrix} .1 = \left(\cos(20^\circ)\cos(10^\circ) - \sin(20^\circ)\sin(10^\circ) = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) & .2 = \left(2\cos(22.5^\circ)^2 - 1 = \left(\cos(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \\ .3 = \left(1 - 2\sin(15^\circ)^2 = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) & .4 = \left(\cos\left(\frac{2\pi}{5}\right)\cos\left(\frac{\pi}{15}\right) + \sin\left(\frac{2\pi}{5}\right)\sin\left(\frac{\pi}{15}\right) = \left(\cos\left(\frac{\pi}{3}\right) = \frac{1}{2} \right) \right) \\ .5 = \left(\sin\left(\frac{13\pi}{36}\right)\cos\left(\frac{\pi}{9}\right) - \cos\left(\frac{13\pi}{36}\right)\sin\left(\frac{\pi}{9}\right) = \left(\sin\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \right) & .6 = \left(\sin\left(\frac{5\pi}{18}\right)\cos\left(\frac{\pi}{18}\right) + \cos\left(\frac{5\pi}{18}\right)\sin\left(\frac{\pi}{18}\right) = \left(\sin\left(\frac{\pi}{3}\right) = \frac{\sqrt{3}}{2} \right) \right) \\ .7 = \left(2\sin\left(\frac{\pi}{8}\right)\cos\left(\frac{\pi}{8}\right) = \left(\sin\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \right) & .8 = \left(\frac{2\tan(15^\circ)}{1 - \tan(15^\circ)^2} = \left(\tan(30^\circ) = \frac{\sqrt{3}}{3} \right) \right) \\ .9 = \left(\frac{\tan(35^\circ) - \tan(5^\circ)}{1 + \tan(35^\circ)\tan(5^\circ)} = \left(\tan(30^\circ) = \frac{\sqrt{3}}{3} \right) \right) & .10 = \left(\cos\left(\frac{\pi}{12}\right)^2 - \sin\left(\frac{\pi}{12}\right)^2 = \left(\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \right) \right) \end{bmatrix}, \begin{bmatrix} \text{.} \\ \text{:} \\ \text{M} \\ \text{a} \\ \text{t} \\ \text{h} \\ \text{.} \\ \text{@} \\ \text{M} \\ \text{U} \\ \text{T} \\ \text{.} \\ \text{:} \\ \text{:} \\ \text{:} \\ \text{:} \\ \text{:} \\ \text{:} \end{bmatrix}$$

$$Ans3 = \begin{bmatrix} .1 = \left(\cos(\alpha) = \frac{\sqrt{5}}{3} \right) & .2 = \left(\sin(\beta) = \frac{\sqrt{15}}{4} \right) \\ .3 = (\tan(\beta) = -\sqrt{15}) & .4 = \left(\sin(\beta - \alpha) = \frac{\sqrt{5}\sqrt{15}}{12} + \frac{1}{6} \right) \\ .5 = \left(\cos(\alpha + \beta) = -\frac{\sqrt{5}}{12} - \frac{\sqrt{15}}{6} \right) & .6 = \left(\tan(\alpha - \beta) = -\frac{32\sqrt{5}}{55} - \frac{9\sqrt{3}\sqrt{5}}{55} \right) \\ .7 = \left(\sin(2\beta) = -\frac{\sqrt{15}}{8} \right) & .8 = (\tan(2\alpha) = 4\sqrt{5}) \end{bmatrix}, Ans4 = \begin{bmatrix} .1 = \left(\sin(\alpha) = -\frac{2\sqrt{6}}{7} \right) & .2 = \left(\cos(\beta) = \frac{\sqrt{35}}{6} \right) \\ .3 = \left(\tan(\beta) = -\frac{\sqrt{35}}{35} \right) & .4 = \left(\sin(\alpha - \beta) = -\frac{\sqrt{6}\sqrt{35}}{21} - \frac{5}{42} \right) \\ .5 = \left(\cos(\alpha + \beta) = -\frac{5\sqrt{35}}{42} - \frac{\sqrt{6}}{21} \right) & .6 = \left(\tan(\beta - \alpha) = -\frac{49\sqrt{35}}{851} - \frac{360\sqrt{6}}{851} \right) \\ .7 = \left(\sin(2\beta) = -\frac{\sqrt{35}}{18} \right) & .8 = (\tan(2\alpha) = 20\sqrt{6}) \end{bmatrix}, \begin{bmatrix} \text{.} \\ \text{:} \\ \text{M} \\ \text{a} \\ \text{t} \\ \text{h} \\ \text{.} \\ \text{@} \\ \text{M} \\ \text{U} \\ \text{T} \\ \text{.} \\ \text{:} \\ \text{:} \end{bmatrix}$$

$$Ans5 = (\sin(34^\circ) = (\text{Sqrt}(0.3125) = 0.559)), \begin{bmatrix} \text{M} \\ \text{U} \\ \text{T} \end{bmatrix}$$

$$Ans6 = (\cos(11^\circ) = (\text{Sqrt}(0.9635) = 0.982)), \begin{bmatrix} \text{M} \\ \text{U} \\ \text{T} \end{bmatrix}$$

$$Ans1 = \begin{bmatrix} .1 = \left(\cos(75^\circ) = \frac{\sqrt{2}\sqrt{3} - \sqrt{2}}{4} \right) & .2 = \left(\sin\left(\frac{\pi}{12}\right) = \frac{\sqrt{2}\sqrt{3} - \sqrt{2}}{4} \right) \\ .3 = (\tan(105^\circ) = -2 - \sqrt{3}) & .4 = \left(\sin\left(-\frac{7\pi}{12}\right) = -\frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .5 = \left(\cos(165^\circ) = -\frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) & .6 = (\csc(-15^\circ) = -\sqrt{2}\sqrt{3} - \sqrt{2}) \\ .7 = \left(\cot\left(\frac{19\pi}{12}\right) = -2 + \sqrt{3} \right) & .8 = (\sec(-345^\circ) = \sqrt{2}\sqrt{3} - \sqrt{2}) \end{bmatrix}$$

$$Ans2 = \begin{bmatrix} .1 = \left(\cos(40^\circ)\cos(20^\circ) - \sin(40^\circ)\sin(20^\circ) = \left(\cos(60^\circ) = \frac{1}{2} \right) \right) & .2 = \left(\cos(40^\circ)\cos(10^\circ) + \sin(40^\circ)\sin(10^\circ) = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) \\ .3 = \left(\cos\left(\frac{\pi}{12}\right)^2 - \sin\left(\frac{\pi}{12}\right)^2 = \left(\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \right) \right) & .4 = (\sin(102^\circ)\cos(12^\circ) - \cos(102^\circ)\sin(12^\circ) = (\sin(90^\circ) = 1)) \\ .5 = \left(2\sin\left(\frac{\pi}{8}\right)\cos\left(\frac{\pi}{8}\right) = \left(\sin\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \right) & .6 = \left(1 - 2\sin(15^\circ)^2 = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) \\ .7 = \left(2\cos(22.5^\circ)^2 - 1 = \left(\cos(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) & .8 = \left(\frac{\tan\left(\frac{\pi}{6}\right) + \tan\left(\frac{\pi}{12}\right)}{1 - \tan\left(\frac{\pi}{6}\right)\tan\left(\frac{\pi}{12}\right)} = \left(\tan\left(\frac{\pi}{4}\right) = 1 \right) \right) \\ .9 = \left(\sin\left(\frac{13\pi}{30}\right)\cos\left(\frac{\pi}{15}\right) + \cos\left(\frac{13\pi}{30}\right)\sin\left(\frac{\pi}{15}\right) = \left(\sin\left(\frac{\pi}{2}\right) = 1 \right) \right) & .10 = \left(\frac{2\tan\left(\frac{\pi}{8}\right)}{1 - \tan\left(\frac{\pi}{8}\right)^2} = \left(\tan\left(\frac{\pi}{4}\right) = \tan\left(\frac{\pi}{4}\right) \right) \right) \end{bmatrix}$$

$$Ans3 = \begin{bmatrix} .1 = \left(\sin(\alpha) = \frac{3\sqrt{5}}{7} \right) & .2 = \left(\cos(\beta) = -\frac{\sqrt{3}}{2} \right) \\ .3 = \left(\tan(\beta) = -\frac{\sqrt{3}}{3} \right) & .4 = \left(\sin(\beta - \alpha) = \frac{1}{7} + \frac{3\sqrt{3}\sqrt{5}}{14} \right) \\ .5 = \left(\cos(\alpha - \beta) = -\frac{\sqrt{3}}{7} + \frac{3\sqrt{5}}{14} \right) & .6 = \left(\tan(\alpha + \beta) = -\frac{8\sqrt{5}}{11} + \frac{49\sqrt{3}}{33} \right) \\ .7 = \left(\sin(2\beta) = -\frac{\sqrt{3}}{2} \right) & .8 = \left(\tan(2\alpha) = -\frac{12\sqrt{5}}{41} \right) \end{bmatrix}, Ans4 = \begin{bmatrix} .1 = \left(\sin(\alpha) = \frac{3}{5} \right) & .2 = \left(\cos(\beta) = \frac{\sqrt{3}}{2} \right) \\ .3 = \left(\tan(\alpha) = \frac{3}{4} \right) & .4 = \left(\sin(\beta - \alpha) = \frac{2}{5} + \frac{3\sqrt{3}}{10} \right) \\ .5 = \left(\cos(\alpha + \beta) = -\frac{2\sqrt{3}}{5} - \frac{3}{10} \right) & .6 = \left(\tan(\alpha - \beta) = \frac{16}{13} + \frac{25\sqrt{3}}{39} \right) \\ .7 = \left(\sin(2\beta) = -\frac{\sqrt{3}}{2} \right) & .8 = \left(\tan(2\alpha) = \frac{24}{7} \right) \end{bmatrix}$$

$$Ans5 = (\cos(17^\circ) = (\text{sqrt}(0.9145) = 0.956)),$$

$$Ans6 = (\sin(4^\circ) = (\text{sqrt}(0.0050) = 0.070)),$$

$$Ans1 = \left[\begin{array}{l} .1 = \left(\cos(105^\circ) = \frac{\sqrt{2}}{4} - \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .2 = \left(\sin\left(\frac{\pi}{12}\right) = \frac{\sqrt{2}\sqrt{3}-\sqrt{2}}{4} \right) \\ .3 = \left(\tan\left(\frac{5\pi}{12}\right) = 2 + \sqrt{3} \right) \\ .4 = \left(\sec\left(-\frac{23\pi}{12}\right) = \sqrt{2}\sqrt{3} - \sqrt{2} \right) \\ .5 = \left(\sin(-285^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \\ .6 = (\cot((-105)^\circ) = 2 - \sqrt{3}) \\ .7 = \left(\csc\left(-\frac{\pi}{12}\right) = -\sqrt{2}\sqrt{3} - \sqrt{2} \right) \\ .8 = \left(\cos(345^\circ) = \frac{\sqrt{2}}{4} + \frac{\sqrt{2}\sqrt{3}}{4} \right) \end{array} \right]$$

$$Ans2 = \left[\begin{array}{l} .1 = \left(2 \sin\left(\frac{\pi}{8}\right) \cos\left(\frac{\pi}{8}\right) = \left(\sin\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2} \right) \right) \\ .2 = \left(\cos\left(\frac{2\pi}{5}\right) \cos\left(\frac{\pi}{15}\right) + \sin\left(\frac{2\pi}{5}\right) \sin\left(\frac{\pi}{15}\right) = \left(\cos\left(\frac{\pi}{3}\right) = \frac{1}{2} \right) \right) \\ .3 = \left(\cos\left(\frac{\pi}{18}\right) \cos\left(\frac{4\pi}{9}\right) - \sin\left(\frac{\pi}{18}\right) \sin\left(\frac{4\pi}{9}\right) = \left(\cos\left(\frac{\pi}{2}\right) = 0 \right) \right) \\ .4 = \left(\cos(15^\circ)^2 - \sin(15^\circ)^2 = \left(\cos(30^\circ) = \frac{\sqrt{3}}{2} \right) \right) \\ .5 = \left(\sin(30^\circ) \cos(15^\circ) + \cos(30^\circ) \sin(15^\circ) = \left(\sin(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \\ .6 = \left(2 \cos\left(\frac{\pi}{12}\right) - 1 = \left(\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \right) \right) \\ .7 = \left(\frac{\tan\left(\frac{\pi}{15}\right) + \tan\left(\frac{\pi}{10}\right)}{1 - \tan\left(\frac{\pi}{15}\right) \tan\left(\frac{\pi}{10}\right)} = \left(\tan\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{3} \right) \right) \\ .8 = \left(1 - 2 \sin(22.5^\circ)^2 = \left(\cos(45^\circ) = \frac{\sqrt{2}}{2} \right) \right) \\ .9 = \left(\frac{\tan(50^\circ) - \tan(20^\circ)}{1 + \tan(50^\circ) \tan(20^\circ)} = \left(\tan(30^\circ) = \frac{\sqrt{3}}{3} \right) \right) \\ .10 = \left(\frac{2 \tan\left(\frac{\pi}{12}\right)}{1 - \tan\left(\frac{\pi}{12}\right)^2} = \left(\tan\left(\frac{\pi}{6}\right) = \tan\left(\frac{\pi}{6}\right) \right) \right) \end{array} \right]$$

$$Ans3 = \left[\begin{array}{l} .1 = \left(\sin(\alpha) = \frac{\sqrt{15}}{4} \right) \\ .2 = \left(\cos(\beta) = -\frac{\sqrt{5}}{3} \right) \\ .3 = \left(\tan(\alpha) = \sqrt{15} \right) \\ .4 = \left(\sin(\beta - \alpha) = \frac{\sqrt{5}\sqrt{15}}{12} + \frac{1}{6} \right) \\ .5 = \left(\cos(\alpha - \beta) = -\frac{\sqrt{5}}{12} + \frac{\sqrt{15}}{6} \right) \\ .6 = \left(\tan(\alpha + \beta) = -\frac{9\sqrt{3}\sqrt{5}}{55} + \frac{32\sqrt{5}}{55} \right) \\ .7 = \left(\sin(2\beta) = -\frac{4\sqrt{5}}{9} \right) \\ .8 = \left(\tan(2\alpha) = -\frac{\sqrt{15}}{7} \right) \end{array} \right], \quad Ans4 = \left[\begin{array}{l} .1 = \left(\cos(\alpha) = -\frac{\sqrt{5}}{3} \right) \\ .2 = \left(\sin(\beta) = -\frac{\sqrt{15}}{4} \right) \\ .3 = \left(\tan(\beta) = -\sqrt{15} \right) \\ .4 = \left(\sin(\beta - \alpha) = \frac{\sqrt{5}\sqrt{15}}{12} + \frac{1}{6} \right) \\ .5 = \left(\cos(\alpha + \beta) = -\frac{\sqrt{5}}{12} - \frac{\sqrt{15}}{6} \right) \\ .6 = \left(\tan(\alpha - \beta) = -\frac{32\sqrt{5}}{55} - \frac{9\sqrt{3}\sqrt{5}}{55} \right) \\ .7 = \left(\sin(2\alpha) = \frac{4\sqrt{5}}{9} \right) \\ .8 = \left(\tan(2\beta) = \frac{\sqrt{15}}{7} \right) \end{array} \right]$$

$$Ans5 = (\sin(20^\circ) = (\text{sqrt}(0.1170) = 0.342)),$$

$$Ans6 = (\cos(39^\circ) = (\text{sqrt}(0.6040) = 0.777)),$$

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